

# Idiosyncratic Volatility, Momentum, Liquidity, and Expected Stock Returns in Developed and Emerging Markets

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This paper re-examines the link between idiosyncratic risk and expected returns for a large sample of firms in both developed and emerging markets. Recent studies using Fama-French three-factor models have shown a negative relationship between idiosyncratic volatility and expected returns for developed markets. This relationship has not been studied to date for emerging markets. This study relates the current-month's idiosyncratic volatility to the subsequent month's stock returns for a sample of both developed and emerging markets expanding benchmark factors by including both a momentum and a systematic liquidity risk component. Using a five-factor model, the results suggest that idiosyncratic risk does not play a role on stock returns for most of the developed markets analyzed. In contrast, the paper shows, for the first time, that idiosyncratic risk is positively related to month-ahead expected returns for many emerging markets for this model. (JEL: G11, G12, G15)

**Keywords:** idiosyncratic volatility; expected returns; developed vs. emerging markets; asset pricing; multifactor models

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## I. Introduction

The seminal papers that introduced the foundations of modern portfolio theory (MPT) (Markowitz (1952); Sharpe (1964); Lintner (1965)) assert that, within the framework of the Capital Asset Pricing Model (CAPM), idiosyncratic risk should not be priced as long as representative agents hold the market portfolio or a well-diversified portfolio. Further theoretical extensions have looked at the effects of risk tolerance, information, and transactions costs in establishing a premium for idiosyncratic volatility (e.g. Levy (1978), Merton (1987), Jones and Rhodes-Kropf (2003), and Malkiel and Xu (2006)).

While the theoretical arguments for an idiosyncratic risk premium are relatively straightforward, the empirical evidence for such a premium is mixed, based on Fama-French type factor models. For example, Fu (2009) provides evidence that high idiosyncratic risk portfolios generate higher returns than low idiosyncratic risk portfolios for the US market. Ang et al. (2006) using monthly data document a negative idiosyncratic effect in US stock markets during the period 1963 to 2000 while Ang et al. (2009) also find a negative idiosyncratic risk effect in 22 developed markets (1980-2003).

This study contributes to the literature by analyzing the behaviour of idiosyncratic risk for an international sample consisting of both developed markets as well as, for the first time, emerging markets stock markets using a five-factor model that incorporates both momentum and liquidity risk. The latter might be deemed of particular importance for emerging markets since poor liquidity is often mentioned as one of the main reasons that prevent foreign investors from investing in emerging markets.

A positive relationship between idiosyncratic volatility and expected returns could imply that some potential risk factors that are not incorporated in the factor models employed in this study are not or may not be completely diversifiable and may hence generate the pricing of idiosyncratic volatility. The international finance literature distinguishes between three categories of non-diversifiable risk factors inherent to emerging markets.

- a) Direct barriers that discriminate against foreign shareholders – which could include ownership restrictions and onerous taxes (see e.g. Stulz (1981)).
- b) Indirect barriers – this would include lack of transparency due to

poor accounting standards, low investor protection (poor corporate governance), high transaction costs, and government expropriation of productive assets (e.g. Carrieri, Chaieb, and Errunza (2013)). Lack of transparency may also be linked to informational inefficiencies. For example, Bhattacharya et al. (2000) show that in emerging markets, insider trading often occurs well before the release of information to the public. Stock prices in such markets respond before public announcements, which is consistent with information leakage. In addition, the price response of shares traded by foreigners lags the price response of shares traded by locals. Another indirect barrier would be related to higher levels of corruption within emerging markets compared to developed markets (Switzer and Tahaoglu (2015)). Many emerging markets may also be prone to agency problems resulting from multilevel (pyramid) ownership structures that facilitate expropriation of the firm's resources by controlling shareholders (Shleifer and Vishny (1997), Lins (2003)). Shareholder rights are generally weak and takeovers are seldom used as an external disciplining governance mechanism (La Porta et al. (1998), Denis and McConnell (2003)).

c) Barriers that result from emerging market specific risks – Clark and Tunaru (2001) for example provide a model that measures the impact of political risk on portfolio investment. They define political risk as the volatility of the exposure of a portfolio to loss in the case of an explicit political event in a given country. Novel feature of their model is that political risk is multivariate and may be correlated across countries. Bekaert et al. (1997) suggest that political risk is priced in several emerging markets. Other emerging market specific risks would also include economic policy risk, and currency risk that dissuade foreign investment. Bartram, Brown and Stulz (2012) provide further insight into market specific factors that may be associated with differences in idiosyncratic volatility between emerging markets and developed markets. They distinguish between “good” volatility (e.g. due to patents, firm-level R&D investment) from “bad” volatility (e.g. linked to political risk and poor disclosure). They conclude that emerging markets are more prone to “bad” volatility factors, relative to developed markets.<sup>1</sup>

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1. They estimate idiosyncratic volatility as the standard deviation of error term from a systematic risk model that explains the return of a stock with the return of its country's market, the world market, and Fama–French size and value factors. Given the high

While Bartram, Brown and Stulz (2012) highlight factors likely associated with good or bad volatility, they do not explore whether or not idiosyncratic volatility per se is priced in the different markets considered. This paper provides new evidence on this score. The analysis uses both the Carhart (1997) four-factor model as well as a five-factor model that incorporates the Amihud (2002) liquidity factor in the estimation of idiosyncratic risk. Using a five-factor model, the results suggest that idiosyncratic risk does not play a role on stock returns for most of the developed markets analyzed. In contrast, the results show, for the first time, that idiosyncratic risk is positively related to month-ahead expected returns for many emerging markets for this model.

Hence this paper presents evidence that the idiosyncratic puzzle found by Ang et al. (2009) in developed markets may be sample period specific. Indeed the negative relationship between expected returns and idiosyncratic volatility, estimated using the Fama-French three-factor model, discovered by Ang et al. (2009) for the period 1980 to 2003 disappears once the sample period is extended to December 2012. The non-existence of the idiosyncratic puzzle observed in this paper corroborates previous papers that have shown the weak evidence of such relationship. For instance, Wei and Zhang (2005) show that a trading strategy based on idiosyncratic volatility does not generate any significant profits in the US stock market during the period 1962 to 2000. Bali et al. (2005) demonstrate that there is no time series relation between idiosyncratic volatility and following stock returns because this relationship is not robust through time, as they show that neither idiosyncratic volatility nor stock market volatility forecasts stock market returns.

Moreover the positive link between idiosyncratic volatility and subsequent monthly returns observed in emerging markets, which rejects the idea of an idiosyncratic puzzle, would be expected according to Levy (1978) and Merton (1987) who assert that investors demand a return compensation for bearing idiosyncratic risk caused particularly by factors that may not be diversifiable. Bartram, Brown and Stulz (2012) enumerate several such risk factors inherent to emerging markets e.g. political risk, liquidity risk, lack of transparency due to poor

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correlations between US and developed market returns and the world market returns, the standard errors of their estimates may be higher than for emerging markets, which could distort the significance of the idiosyncratic volatility factor. This problem is highlighted in Girard and Sinha (2006) who show that unlike developed markets, emerging markets are sensitive to local, but not global risk factors.

accounting standards and informational inefficiencies and low investor protection.

In order to estimate idiosyncratic volatility, the four-factor model, which is an extension to the Fama-French three-factor model by adding a momentum factor, and the five-factor model, which incorporates a liquidity risk factor to the previous model, are employed. A liquidity risk factor is included in this study since it is generally recognised that liquidity is important for asset pricing and that systematic variation in liquidity matters for expected returns: Since rational investors require a higher risk premium for holding illiquid securities, these assets and assets with high transaction costs are characterized by low prices relative to their expected cash flows i.e. average liquidity is priced (Amihud and Mendelson (1986); Brennan and Subrahmanyam (1996); Chordia, Roll and Subrahmanyam (2001)). For instance, Haugen and Baker (1996) document that the liquidity of stocks is one of several common factors in explaining stock returns across global markets. Amihud, Mendelson, and Lauterbach (1997) show that enhancement in liquidity on the Tel Aviv Stock Exchange is linked to price increases.

This paper examines the issue of liquidity for developed countries but as well as for a set of markets where liquidity ought to be particularly important i.e. emerging markets. Two reasons show that laying emphasis on illiquidity is critical for emerging markets due to their limited access to global capital markets. Firstly, returns in emerging countries may be adversely affected by the increased illiquidity of trading stocks relative to returns in more developed markets. Secondly Bekaert, Harvey and Lundblad (2007) show results suggesting that local market liquidity is an important driver of expected returns (liquidity is a priced factor), much more so than local market risk, in emerging markets and that model specifications that incorporate liquidity risk outperform other models that only consider market risk factors in predicting future returns. Moreover Bekaert, Harvey and Lundblad (2007) document that higher political risk and weak law and order conditions could act as segmentation indicators and that liquidity may further affect expected returns in countries with these aspects. The authors explain that liquidity effects are relatively small in a developed country such as the United States since its market is large in the number of traded securities and because it has a very diversified ownership structure i.e. a stock market categorized by both long-horizon investors, less prone to liquidity risk, and short-term investors. Hence, in the United States clientele effects in portfolio choice alleviate the pricing of liquidity while such variety in securities and ownership is deficient

in emerging markets, potentially reinforcing liquidity effects. Lesmond (2005) corroborates Bekaert, Harvey and Lundblad's (2007) findings by investigating the impact of legal origin and political institutions on liquidity levels provide evidence that countries with poor political and legal systems and organizations have considerably greater liquidity costs than do countries with solid and strong political and legal institutions. Higher incremental political risk translates into a 1.9% increase in price impact costs employing the Amihud measure.

The remainder of this study is organized as follows. In the next section, a review of the literature is presented. An introduction of the data used in this paper and a description of the research methodology is provided in section III. The empirical results follow in section IV. The paper concludes with a summary in section V.

## II. Literature Review

Idiosyncratic volatility has been a topic of considerable interest in the literature since the seminal contributions of Levy (1978) and Merton (1987) and the empirical results of Campbell et al. (2001) that show a secular increase in idiosyncratic volatility over a long horizon. Merton (1987) argues that to the extent that investors cannot create portfolios that contain only systematic risk they demand a return compensation for bearing idiosyncratic risk: the less diversified the portfolios, the higher the proportion of idiosyncratic risk impounded into expected returns making high idiosyncratic stocks earn more than low idiosyncratic stocks – i.e. idiosyncratic risk should be positively related to stock returns. However, no consensus has emerged on the actual effects of idiosyncratic volatility on the cross-sectional variation in stock returns. Some studies have found a positive relationship, consistent with Merton (1987). Others have shown either no relationship or even a negative relationship between idiosyncratic risk and stock returns.

### *A. Positive relationship between idiosyncratic volatility and stock returns*

Malkiel and Xu (1997) form portfolios of US stocks based on idiosyncratic volatility and show a positive relationship between idiosyncratic volatility and the cross-section of monthly future stock returns. Goyal and Santa-Clara (2003) also find that average stock

idiosyncratic volatility is positively related to value-weighted market returns. Similar results are shown by Wei and Zhang (2005), and Pukthuanthong-Le and Visaltanachoti (2009). Fu (2009) shows that forecasts of idiosyncratic volatility based on exponential generalized autoregressive conditional heteroskedasticity (EGARCH) models are positively related to returns from 1963 to 2006. Bainbridge and Galagedera (2009) show evidence of a positive relationship between idiosyncratic volatility and expected stock returns for Australian stocks. Ben-David, Franzoni and Moussawi (2012) present evidence that hedge funds generate higher returns from trading high idiosyncratic risk stocks rather than low idiosyncratic risk stocks. Nartea, Ward, and Yao (2011) show a positive relationship between idiosyncratic volatility and expected stock returns in four Southeast Asian stock markets (i.e. Singapore, Malaysia, Indonesia, and Thailand) during the period from the early 1990s to the end of 2007. More recently, Brooks, Li, and Miffre (2013) show that cross-sectional returns are positively related to differences in the unsystematic risk of portfolio returns. Their finding is that idiosyncratic risk is priced. In sum, these papers are in line with the notion that agents who fail to fully diversify their portfolios demand higher average returns to compensate them for bearing higher levels of firm-specific risk (Merton (1987)).

*B. Negative relationship between idiosyncratic volatility and stock returns*

Ang et al. (2006) provide empirical evidence suggesting that U.S. stocks with higher lagged idiosyncratic volatility have abnormally lower equally-weighted returns, a phenomenon which they call “the idiosyncratic risk puzzle.” The authors report that the average return differential between the lowest and highest quintile portfolios formed on one-month lagged idiosyncratic volatilities is about  $-1.06\%$  per month for the period 1963-2000. In their paper, idiosyncratic volatility is measured as the standard deviation of the residuals of the daily three-factor Fama and French (1993) model over the prior month. Guo and Savickas (2006) show that value-weighted idiosyncratic volatility is negatively and significantly related to subsequent quarterly excess stock market returns, for G7 countries using quarterly data over the period 1963 to 2002. Chang and Dong (2006) document a negative relationship between idiosyncratic volatility and expected stock returns in the Japanese stock market from 1975 to 2002. Koch (2010) finds that

low idiosyncratic volatility stocks generate higher returns than high idiosyncratic volatility stocks in the German stock market from 1974 to 2006.

*C. No relationship between idiosyncratic volatility and stock returns*

Wei and Zhang (2005) demonstrate that a trading strategy based on idiosyncratic volatility does not yield any significant economic gains using US stock market data over the period 1962 to 2000. Bali et al. (2005) argue that the findings of Goyal and Santa-Clara (2003) that the average idiosyncratic risk is positively related to future returns are not robust through time. They conclude that there is no time series relation between diversifiable risk and subsequent stock returns, as they show that neither idiosyncratic volatility nor stock market volatility forecasts stock market returns in an extended sample ending in 2001. Bali and Cakici (2008) state that the relationship between idiosyncratic volatility and the cross-section of stock returns largely depends on the data frequency used to compute asset-specific volatility. Nardea and Ward (2009) report that there is no association between diversifiable volatility and expected stock portfolio returns in the Philippine stock market.

Huang et al. (2010) suggest that the disparate results for Bali and Cakici (2008) and Ang et al. (2009) can be explained by short term monthly return reversals – which could confound the results of conventional three or four-factor models of expected returns. On balance, they suggest that no relationship between idiosyncratic return and risk should be observed once return reversals are accounted for.

In a recent paper, Fan, Opsal, and Yu (2015) show that idiosyncratic risk across several international equity markets is correlated with abnormal returns associated with a wide array of stock market anomalies, including asset growth, book-to-market, investment-to-assets, momentum, net stock issues, size, and total accruals, in international equity markets. They find that idiosyncratic risk has less impact on abnormal returns associated with anomalies in developed countries than on emerging countries. However, they do not look at how idiosyncratic returns are associated with expected returns per se.

In sum, the evidence to date concerning the relationship between idiosyncratic volatility and stock returns remains ambiguous. Furthermore, most existing empirical research focuses on US stock markets, and is based on simple applications of basic factor models (e.g.



the one factor model or the three-factor Fama-French (1993) model), or time series approaches (such as GARCH) that are not directly linked to asset pricing models. This paper looks to extend our understanding of the role of idiosyncratic risk and volatility by a) providing more recent evidence from other developed and emerging stock markets; and b) using further extensions to the Fama-French (1993) model that may improve the measurement of idiosyncratic risk.

### **III. Data and Methodology**

This study uses stock market daily returns on firms from 23 developed and 15 emerging markets: Argentina, Australia, Austria, Belgium, Brazil, Canada, Denmark, Finland, France, Germany, Greece, Hong Kong, India, Indonesia, Ireland, Israel, Italy, Japan, Korea, Malaysia, Mexico, the Netherlands, New Zealand, Norway, Philippines, Poland, Portugal, Russia, Singapore, South Africa, Spain, Sweden, Switzerland, Taiwan, Thailand, Turkey, the UK and the US. Non-US firm returns are collected from the Thompson Financial Datastream for the sample period January 1980 to December 2012. US stock returns are obtained from CRSP. Because the Czech Republic, which was initially included in the sample, never reaches the threshold of 30 stocks during the sample period analysed this country is removed from the study. We consider the returns from local investor or currency hedged foreign investor perspectives by studying local-currency denominated returns for the analyses, with excess returns computed using each country 1-month or 3-month T-Bill rates.<sup>2</sup> As per Ang et al. (2009), in all non-U.S. countries, we exclude very small firms by eliminating the 5% of firms with the lowest market capitalizations. The number of stocks included and the coverage period for each country are shown in table 1. A set of illustrative stocks in various countries used in the analyses is provided in appendix 1.<sup>3</sup>

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2. For nations in which the 1-month or 3-month T-Bill rates are not available the 1 month U.S. T-Bill rate was used as per Ang et al. (2009). Note also that for countries in which the 1-month or 3-month T-Bill rates were obtainable, idiosyncratic volatilities were computed twice using both local rates and the 1-month U.S. T-Bill rate giving similar results for each country.

3. A complete listing of stocks for all countries used in the analyses is available on request.

**TABLE 1. Description of Sample: Distribution of Stocks by Country**

Country	Start	N(Start)	End	N(End)
<b>G7 Countries</b>				
Canada	Jan 1980	32	Dec 2012	233
France	Jan 1980	34	Dec 2012	233
Germany	Jan 1980	47	Dec 2012	233
Italy	Jun 1986	35	Dec 2012	149
Japan	Jan 1980	319	Dec 2012	916
United Kingdom	Jan 1980	388	Dec 2012	911
United States	Jan 1980	1978	Dec 2012	3788
<b>Developed Markets</b>				
Australia	Jan 1984	30	Dec 2012	152
Austria	Jun 1999	30	Dec 2012	46
Belgium	Jun 1986	30	Dec 2012	83
Denmark	Jun 1992	30	Dec 2012	42
Finland	Jul 1994	30	Dec 2012	46
Greece	Jul 1998	30	Dec 2012	47
Hong Kong	Jun 1988	35	Dec 2012	122
Ireland	Dec 2007	30	Dec 2012	30
Netherlands	Jan 1980	34	Dec 2012	105
New Zealand	Sep 1999	30	Dec 2012	45
Norway	Jun 2001	30	Dec 2012	47
Portugal	Jun 1998	30	Dec 2012	46
Singapore	Feb 1989	30	Dec 2012	93
Spain	Jun 1999	30	Dec 2012	46
Sweden	Aug 1991	30	Dec 2012	66
Switzerland	Jul 1980	30	Dec 2012	133
<b>Emerging Markets</b>				
Argentina	Jan 1995	30	Dec 2012	50
Brazil	Oct 1994	30	Dec 2012	97
India	Nov 1994	93	Dec 2012	198
Indonesia	Jun 1998	30	Dec 2012	50
Israel	Jun 1996	30	Dec 2012	50
Korea	May 1987	31	Dec 2012	97
Malaysia	Jan 1986	30	Dec 2012	89
Mexico	Mar 1993	30	Dec 2012	84
Philippines	Nov 1994	30	Dec 2012	50
Poland	Apr 2005	30	Dec 2012	50
Russia	Jan 2007	30	Dec 2012	47
South Africa	Jan 1990	34	Dec 2012	70
Taiwan	Nov 1994	30	Dec 2012	70
Thailand	Aug 1994	30	Dec 2012	50
Turkey	Apr 1997	30	Dec 2012	49

**Note:** This table presents data coverage of the G7 countries, 16 developed markets and 15 emerging markets. N(start) and N(end) show the number of stocks at the starting and ending sample period.

### A. Estimating idiosyncratic volatilities

This paper uses an intertemporal approach in which lagged monthly idiosyncratic volatility is related to monthly returns. Ang et al. (2006, 2009) measure idiosyncratic risk by realized idiosyncratic volatility using a local version of the Fama and French (1993) three-factor model (1). The idiosyncratic volatility of a stock in each month is the standard deviation of the regression residuals  $\varepsilon_i$ :

$$r_i = \alpha_i + \beta_i MKT + s_i SMB + h_i HML + \varepsilon_i \quad (1)$$

where  $r_i$  is the daily excess returns of stock  $i$ ,  $\alpha_i$  is the Fama–French adjusted alpha,  $MKT$  is the excess return on the market portfolio in each country defined as the value-weighted average of all stocks;  $SMB$  (small minus big market capitalization) and  $HML$  (high minus low book-to-market) are return differences between the top 33.33 percent and bottom 33.33 percent ranked stocks in each country respectively;  $\beta_i$ ,  $s_i$  and  $h_i$  are the estimated factor exposures. Griffin (2002) provides evidence that the Fama and French factors are country specific and concludes that the three-local factor Fama-French model provides a better explanation of time-series variation in stock returns for international stocks than a global factor model.

This study extends the three-factor model by adding two additional factors to estimate idiosyncratic volatilities: a momentum factor and an illiquidity factor. We perform the analyses using both the Carhart (1997) model (equation (2)) that incorporates momentum, as well as a five-factor model (equation (3)) that includes an illiquidity premium as well:

$$r_i = \alpha_i + \beta_i MKT + s_i SMB + h_i HML + m_i MOM + \varepsilon_i \quad (2)$$

$$r_i = \alpha_i + \beta_i MKT + s_i SMB + h_i HML + m_i MOM + l_i IML + \varepsilon_i \quad (3)$$

Analogous to the size ( $SMB$ ), and the book-to-market ( $HML$ ) return proxies, the momentum factor ( $MOM$ ) is constructed as the equal-weighted average of firms with the highest 33.33 percent eleven-month returns lagged one month minus the equal-weighted average of firms with the lowest 33.33 percent eleven-month returns lagged one month (Carhart (1997)).

The illiquidity premium denoted  $IML$  (illiquid-minus-liquid portfolio

return) is the difference between the average excess return on high-illiquidity stocks (33.33 percent highest) and low-illiquidity stocks (33.33 percent lowest). In this study the proxy used for illiquidity is the “price impact” illiquidity measure proposed by Amihud (2002). This measure captures the response associated with one dollar of trading volume. More specifically, the illiquidity factor is computed as the daily ratio of absolute stock return to dollar volume:

$$Illiq_i = \frac{|r_i|}{DVOL_i} \quad (4)$$

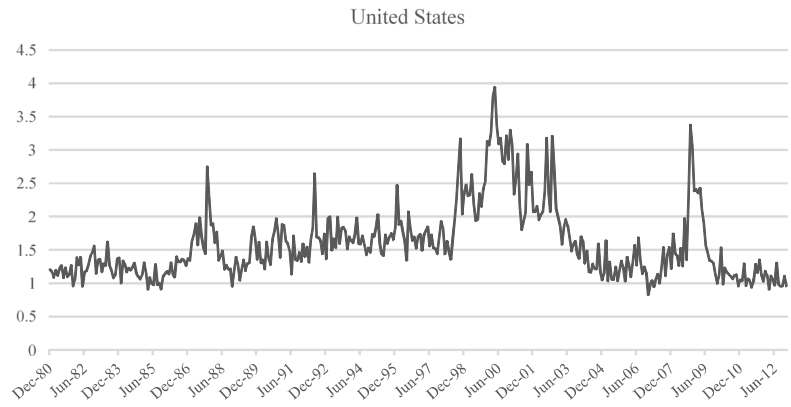
where  $r_i$  is a daily stock return of stock  $i$ , and  $DVOL_i$  is daily dollar volume.

We use the illiquidity measure proposed by Amihud (2002) since it is one of the most widely used in the finance literature. This popularity is due to two advantages it has over many other liquidity measures. First, the measure can be easily constructed using daily stock data. Second, the measure shows a strong positive relationship with a high-frequency price impact measure and expected stock return (e.g. Amihud (2002), and Chordia, Huh, and Subrahmanyam (2009)).

The trading strategy based on idiosyncratic volatility involves portfolios formation based on an estimation period of  $L$  months, a waiting period of  $M$  months, and a holding period of  $N$  months. The  $L/M/N$  strategy is defined as follows. At month  $t$ , idiosyncratic volatilities from regressions (3) and (4) on daily data over an  $L$ -month period from month  $t - L - M$  to month  $t - M$  are measured. At time  $t$ , portfolios based on these idiosyncratic volatilities are formed and held for  $N$  months. In this study, the analysis focuses on the 1/0/1 strategy, in which stocks are sorted into quintile portfolios based on their level of idiosyncratic volatility estimated using daily returns over the previous month, and held for 1 month. The portfolios are reformed at the beginning of each month.

#### IV. Empirical Results

Figure 1 provides graphs of the time variation of aggregate idiosyncratic volatility for the United States, G7 countries (except Italy), developed markets and emerging markets all depict no significant positive trend



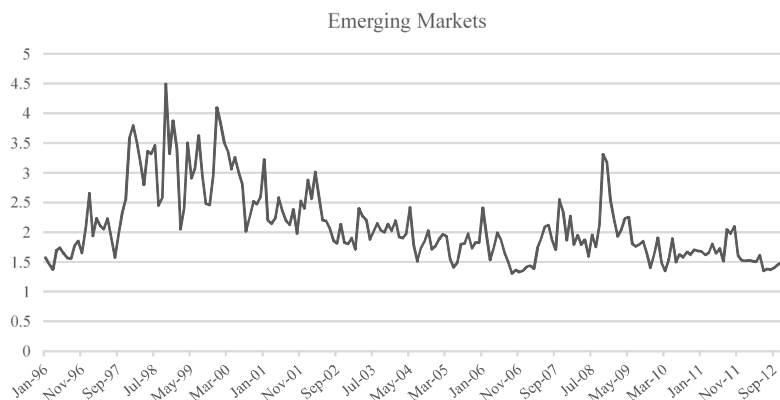


FIGURE 1.— Time Series Plots of Aggregate Monthly Idiosyncratic Volatility (%) – based on four-factor model

**Note:** Developed Markets: Australia, Belgium, Denmark, Hong Kong, Netherlands, Singapore, Sweden and Switzerland. Emerging Markets: Argentina, Brazil, India, Korea, Malaysia, Mexico, Philippines, South Africa, Taiwan and Thailand.

over the full sample period.

The positive trend in idiosyncratic volatility observed by Campbell et al. (2001) for the period ending 1997 continues until June 2000, but is not clearly evident thereafter. It is also noteworthy that for the US, three out of the seven peaks in the aggregate levels of idiosyncratic volatility occur during the October 1987 crash, the March 2000 technology bubble burst, and the fall 2008 global financial crisis. Spikes in idiosyncratic volatility are also observed for other G-7 and developed markets as well as for emerging markets during March 2000 and Fall 2008.

Table 2 reports summary statistics for three different average volatility measures of stock returns across countries: idiosyncratic volatilities measured based on the four-factor model, the five-factor model, and total volatility which is computed as the volatility of daily raw returns over the previous month; the volatility measures are all annualized by multiplying by  $\sqrt{250}$ .

New Zealand has the lowest idiosyncratic volatility (20.50% per annum based on the four-factor model and 19.08% using the five-factor model) while Ireland shows the highest idiosyncratic volatility (42.87%

per annum measured on the four-factor model and 39.99% measured on the five-factor model). The average idiosyncratic volatilities for G7 Countries are 29.26% and 28.05% based on the four-factor and five-factor models respectively. The estimates of idiosyncratic volatility are lower for developed markets (27.97% and 26.63%) but higher for emerging markets (30.45% and 28.45%), perhaps reflecting the direct and indirect barriers to foreign investors, as well as country specific risks that are of greater significance for emerging markets.

Tables 3 and 4 (tables 5 and 6) show the results for the returns of equal-weighted (value-weighted) portfolios sorted on past 1-month idiosyncratic volatility for all countries measured based on the five-factor and four-factor models respectively; Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities.

A negative relationship between idiosyncratic volatility and portfolio future returns in each of the non-U.S. G7 countries (Panel A) is observed, using both equal- and value-weighted portfolios, consistent with Ang et al. (2009) for the full period from January 1980 to December 2012 (except for Italy which starts in June 1986). However, the US (equally-weighted) and the United Kingdom (value-weighted) are the only G7 countries that exhibit a positive relationship between asset-specific risk and expected monthly returns which contrasts with Ang et al. (2006, 2009).

However, two critical facts in these figures deserve attention. First none of the G7 countries display a monotonic idiosyncratic volatility –returns relationship across portfolios ranked from the lowest idiosyncratic risk portfolio (Quintile 1) to the highest (Quintile 5). Average returns decline from Quintile 1 to Quintile 2 for Canada, France, Germany, Italy and Japan and then increase as we move from portfolio 2 to portfolio 5, as is shown in appendix 2. Using equal-weighted portfolios, the difference of returns between Quintile 1 and Quintile 5 is significant for only three countries: France, Germany and Japan, amounting to 1.57, 1.06 and 1.24 percent per month respectively based on the five-factor model.<sup>4</sup>

For value-weighted portfolios, the results are even more attenuated: the relationships between idiosyncratic volatility and expected returns

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4. The estimates are 1.60, 1.04 and 1.24 percent per month when diversifiable risk is estimated using the four-factor model, and are statistically significant at conventional levels.

TABLE 2. Descriptive Statistics

Country	N(End)	Number of Months	Total Volatility (%)	Idiosyncratic Volatility (%) Four-Factor Model	Idiosyncratic Volatility (%) Five-Factor Model
A. G7 Countries					
Canada	233	396	59.28	37.67	35.95
France	233	396	43.92	28.80	27.54
Germany	233	396	39.15	31.90	30.81
Italy	149	319	36.98	25.06	23.95
Japan	916	396	38.08	28.55	27.36
United Kingdom	911	396	31.55	24.25	23.11
United States	3788	396	40.08	28.60	27.53
B. Developed Markets					
Australia	152	348	37.48	26.92	25.78
Austria	46	163	32.78	22.50	21.31
Belgium	83	319	32.85	24.24	22.98
Denmark	42	247	39.94	23.02	21.76
Finland	46	222	37.56	26.08	24.51
Greece	47	174	45.97	28.49	26.44
Hong Kong	122	295	55.08	28.85	30.36
Ireland	30	61	85.16	42.87	39.99
Netherlands	105	396	45.18	30.41	28.84
New Zealand	45	160	30.00	20.50	19.08

(Continued)



**TABLE 2. (Continued)**

Country	N(End)	Number of Months	Total Volatility (%)	Idiosyncratic Volatility (%) Four-Factor Model	Idiosyncratic Volatility (%) Five-Factor Model
<b>B. Developed Markets</b>					
Norway	47	139	43.52	28.66	26.96
Portugal	46	175	69.23	35.90	33.69
Singapore	93	287	38.42	32.33	31.15
Spain	46	163	41.10	29.60	28.15
Sweden	66	257	35.91	23.43	22.32
Switzerland	133	390	30.92	23.82	22.77
<b>C. Emerging Markets</b>					
Argentina	50	216	70.62	32.80	28.48
Brazil	97	219	67.36	33.18	31.17
India	198	218	59.89	36.60	35.32
Indonesia	50	175	77.30	39.14	36.20
Israel	50	199	41.28	27.63	25.81
Korea	97	308	53.27	33.65	31.43
Malaysia	89	324	41.37	26.21	24.82
Mexico	84	238	55.05	26.10	24.47
Philippines	50	218	47.65	34.58	31.70
Poland	50	93	49.50	27.76	26.29
Russia	47	72	73.35	31.49	28.78

(Continued)

TABLE 2. (Continued)

Country	N(End)	Number of Months	Total Volatility (%)	Idiosyncratic Volatility (%) Four-Factor Model	Idiosyncratic Volatility (%) Five-Factor Model
C. Emerging Markets					
South Africa	70	276	42.48	26.43	25.20
Taiwan	70	218	40.78	23.56	22.58
Thailand	50	221	60.94	31.30	29.52
Turkey	49	189	45.12	26.29	25.01

**Note:** This table summarizes the time-series statistics of individual stock idiosyncratic volatilities. N(end) denotes the number of stocks at the ending sample period. The column "Number of months" reports the number of monthly observations for each country. The column "Total Volatility" is the mean of the standard deviation of daily returns. The columns "Idiosyncratic Volatility Four-Factor Model" and "Idiosyncratic Volatility Five-Factor Model" report the mean of idiosyncratic volatilities computed in reference to the four-factor and five-factor model respectively. Average time series of volatilities in each country are expressed in annualized terms by multiplying by  $\sqrt{250}$ .

are weaker and only two countries: Canada and Germany show a statistically significant relationship when idiosyncratic volatility is measured based on the five-factor model. Germany appears to be the country with the most significant results amongst the G7 countries, and shows a monotonic (negative) relationship between idiosyncratic volatility and stock market return performance. The results are consistent with Koch (2010) who also shows that the idiosyncratic volatility puzzle in Germany cannot be explained by return reversals (as per Huang et al (2010)). Germany has long been known as having one of the most bank-based financial systems relative to other countries in the G-7. The relatively “thinner” equity market of German firms may in part explain the idiosyncratic volatility puzzle for Germany. Providing a more thorough rational explanation of this result remains a matter for future research, however.

Panels B of tables 3 to 6 display results for developed markets and provide mixed evidence on the relationship between idiosyncratic risk and monthly expected returns. Indeed, for equal-weighted portfolios, 5 (11) developed markets show a negative (positive) relationship between idiosyncratic volatility and monthly expected returns but none of the differences in mean are statistically significant. For value-weighted portfolios, the results remain almost identical: 2 (14) developed markets (when idiosyncratic volatility is estimated in respect to the five-factor model) and 5 (11) developed markets (when idiosyncratic volatility is estimated in respect to the four-factor model) suggest a negative (positive) relationship between idiosyncratic volatility and monthly expected returns. Moreover, as per the results regarding G7 countries, a monotonic relationship from Quintile 1 to Quintile 5 is not observed for any of the developed countries in the sample.

The results for emerging countries shown in Panel C of tables 3 to 6, contrast with those of the G-7 and developed countries. While most of the G7 countries show a negative association between diversifiable risk and expected returns, emerging countries exhibit an opposite relation: 12 out of these 15 countries suggest a positive link between idiosyncratic risk and expected returns. Furthermore, contrary to both developed and G7 countries, with the exception of Israel, Russia, and Thailand, the relationship between returns and idiosyncratic volatility appears to be fairly linear. Whether estimating idiosyncratic volatility with the four or the five-factor model, the results in tables 3 to 6 show

TABLE 3. Countries Idiosyncratic Volatility in reference to the Five-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>A. G7 Countries</b>						
Canada	2.90	1.33	1.22	1.32	2.29	0.61
France	2.67	0.67	0.86	0.93	1.11	1.57**
Germany	2.04	0.88	1.03	0.89	0.98	1.06**
Italy	2.17	0.14	0.83	0.37	0.62	1.55
Japan	1.64	0.17	0.09	0.26	0.39	1.24***
United Kingdom	1.21	1.03	0.92	1.09	1.05	0.16
United States	1.62	1.45	1.25	1.22	1.68	-0.06
<b>B. Developed Markets</b>						
Australia	2.31	1.44	0.89	1.35	1.61	0.69
Austria	0.89	0.65	0.75	0.89	1.02	0.13
Belgium	1.21	1.01	0.79	0.71	0.60	0.61
Denmark	1.07	0.79	0.94	1.25	1.61	-0.55
Finland	0.37	0.83	0.62	1.09	1.46	-1.08
Greece	0.83	2.45	1.37	1.35	2.12	-1.29
Hong Kong	2.26	2.25	1.50	1.83	2.17	0.09
Ireland	1.36	1.01	1.02	1.33	1.13	0.23
Netherlands	1.30	0.61	0.61	0.82	0.29	1.01
New Zealand	1.29	0.69	0.87	0.99	0.91	0.38
Norway	1.39	2.07	1.79	2.00	1.23	0.17
Portugal	-1.25	-0.57	0.44	0.94	0.98	-2.23

(Continued)

TABLE 3. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	3.18	1.12	1.19	1.13	1.33	1.85
Spain	-0.0119	0.0003	-0.0015	-0.0003	0.0193	-0.0312
Sweden	2.04	1.20	0.87	1.24	1.58	0.45
Switzerland	1.24	0.93	0.73	0.76	0.93	0.31
<b>C. Emerging Markets</b>						
Argentina	0.31	0.24	0.31	1.45	4.58	-4.27***
Brazil	0.11	1.84	2.19	2.06	2.59	-2.48***
India	1.63	2.50	2.00	2.22	2.56	-0.93
Indonesia	-0.48	0.45	0.56	2.16	6.75	-7.23***
Israel	1.15	1.09	10.02	1.78	2.34	1.19
Korea	0.15	1.47	1.67	1.65	2.21	-2.06***
Malaysia	0.78	0.84	0.84	1.70	2.15	-1.36
Mexico	1.04	0.88	2.24	2.73	2.69	-1.66
Philippines	2.20	2.33	1.82	1.89	3.91	-1.71
Poland	1.82	1.44	1.68	1.31	1.71	0.11
Russia	1.18	2.57	1.35	2.43	3.62	-2.44***
South Africa	1.77	1.75	1.60	1.74	2.15	-0.38
Taiwan	0.82	0.37	0.72	1.23	1.79	-0.97

(Continued)

TABLE 3. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Thailand	1.41	0.43	1.72	1.85	2.40	-0.99
Turkey	2.18	2.12	2.06	1.78	1.45	0.73

**Note:** Equal-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the five-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column “Q1–Q5” reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

TABLE 4. Countries Idiosyncratic Volatility in reference to the Four-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>A. G7 Countries</b>						
Canada	2.96	1.34	1.23	1.25	2.33	0.63
France	2.68	0.65	0.86	0.95	1.09	1.60**
Germany	2.02	0.82	1.04	0.92	0.98	1.04**
Italy	2.22	0.11	0.82	0.38	0.61	1.61
Japan	1.63	0.18	0.11	0.23	0.39	1.24***
United Kingdom	1.22	1.04	0.92	1.08	1.05	0.17
United States	1.76	1.78	1.25	1.42	1.73	0.03
<b>B. Developed Markets</b>						
Australia	2.13	1.47	0.85	1.38	1.62	0.51
Austria	0.84	0.56	0.91	0.86	1.98	-0.15
Belgium	1.07	1.09	0.80	0.62	0.65	0.43
Denmark	1.24	0.99	0.91	1.19	1.65	-0.41
Finland	0.34	0.75	0.56	1.15	1.51	-1.17
Greece	0.82	2.39	1.95	1.81	2.04	-1.22
Hong Kong	2.31	2.20	1.54	1.80	2.18	0.13
Ireland	1.56	1.11	0.36	1.65	1.16	0.40
Netherlands	1.20	0.68	0.56	0.87	0.27	0.93
New Zealand	1.46	0.84	0.88	0.97	0.86	0.59
Norway	1.37	2.14	1.81	1.90	1.30	0.07
Portugal	-1.34	-0.40	0.46	0.87	1.02	-2.36

(Continued)

TABLE 4. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	3.23	1.05	1.26	1.14	1.34	1.89
Spain	-0.011	0.0018	0.0021	0.0003	0.0019	-0.0313
Sweden	2.09	1.11	1.01	1.24	1.54	0.55
Switzerland	1.23	0.94	0.70	0.81	0.92	0.32
<b>C. Emerging Markets</b>						
Argentina	0.15	0.36	0.21	1.37	4.65	-4.51***
Brazil	-0.04	1.75	2.22	2.19	2.49	-2.54***
India	1.63	2.50	2.00	2.22	2.56	-0.93
Indonesia	-0.53	0.41	0.36	2.19	6.90	-7.43***
Israel	1.21	1.05	1.49	7.70	2.31	-1.10
Korea	0.15	1.47	1.67	1.65	2.21	-2.06***
Malaysia	0.61	0.90	0.93	1.77	2.05	-1.44
Mexico	1.20	0.81	1.80	3.01	2.70	-1.50*
Philippines	1.98	2.93	1.45	1.97	4.09	-2.11***
Poland	1.67	1.62	1.82	1.21	1.71	-0.04
Russia	1.28	2.19	2.21	2.36	3.28	-2.00***
South Africa	1.87	1.46	1.78	1.65	2.19	-0.33

(Continued)



**TABLE 4. (Continued)**

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Taiwan	0.92	0.29	0.93	1.13	1.78	-0.86
Thailand	1.40	0.38	1.50	2.02	2.42	-1.02
Turkey	1.99	2.05	2.01	1.93	1.52	0.47

**Note:** Equal-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the four-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column “Q1 – Q5” reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

a strong and statistically significant difference in means (for both equal- and value-weighted portfolios) between the two extreme quintiles for 5 out of the 15 emerging countries: Argentina, Brazil, Indonesia, Korea and Russia for equal-weighted portfolios and the same countries for value-weighted portfolios except that Russia is replaced by The Philippines.

One possible reason that the results differ between G7 countries and emerging markets could be because of differences in the level of portfolio diversification attained by investors. Indeed, the results for emerging countries corroborate theories assuming investor under-diversification caused by market frictions that prevent investing in fully diversified portfolios (Levy (1978), Merton (1987)); in such an environment investors request compensation for bearing idiosyncratic risk generating a positive relationship between idiosyncratic volatility and returns.

Other factors that could have affected differences between G7 countries and emerging markets results comprise differences in terms of degrees of financial liberalization (Umutlu, Akdeniz, and Altay-Salih (2010)), financial market development (Brown and Kapadia (2007)), and the degree of investor protection (Lemmon and Lins (2003); Cheng and Shiu (2007)).

Tables 7 and 8 report comparative results for portfolio returns when idiosyncratic volatility is computed using three-factor model for equal- and value-weighted portfolios respectively. Again an overall similar pattern is observed when comparing these results with the ones derived from the four and five-factor models. Only 3 (equal-weighted) and 2 (value-weighted) out the G7 countries suggest a strong negative relationship between specific volatility and expected returns.

For developed markets, we also obtain similar general results when idiosyncratic volatility is estimated using the three, four and five-factor models: no statistically significant relationship is observed except for Australia (value-weighted portfolios). However it is interesting to notice that 9 out of the 16 countries show a negative relationship for the value-weighted portfolios but only 4 out of these same countries suggest the same direction of relationship for equal-weighted portfolios. Note that in their paper, Ang et al. (2009) employ the three-factor model as well as value-weighted portfolios to obtain a negative association between idiosyncratic volatility and expected returns for G7 and

TABLE 5. Countries Idiosyncratic Volatility in reference to the Five-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
A. G7 Countries						
Canada	1.78	0.41	0.99	0.92	0.30	1.48**
France	0.48	-0.12	0.47	0.01	-0.13	0.61
Germany	2.82	1.83	0.79	0.03	1.13	1.69**
Italy	1.41	0.18	0.58	0.59	1.23	0.18
Japan	1.50	0.61	0.67	0.75	1.23	0.27
United Kingdom	0.43	0.24	0.40	0.70	0.60	-0.16
United States	1.34	0.53	0.64	1.00	1.45	-0.11
B. Developed Markets						
Australia	1.92	1.42	-1.79	2.74	2.05	-0.13
Austria	-0.01	0.55	0.55	1.29	1.46	-1.47
Belgium	1.14	-0.10	0.03	1.30	1.34	-0.20
Denmark	1.28	1.00	1.36	0.57	0.79	0.49
Finland	0.04	2.13	1.50	1.33	1.10	-1.06
Greece	0.32	1.00	1.28	1.59	2.16	-1.84
Hong Kong	2.28	1.37	1.17	2.23	2.85	-0.67
Ireland	1.63	1.21	1.21	1.96	2.11	-0.48
Netherlands	1.67	0.42	0.90	1.52	1.87	-0.20
New Zealand	1.19	0.90	0.68	-0.33	0.89	0.30
Norway	0.21	1.93	1.44	2.03	1.63	1.42
Portugal	-1.12	0.01	1.23	0.79	1.30	-2.42

(Continued)

TABLE 5. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	2.59	1.17	0.98	1.06	1.69	-0.90
Spain	-0.008	0.009	0.011	0.010	0.008	-0.016
Sweden	1.51	1.09	1.10	1.29	2.37	-0.86
Switzerland	0.91	0.91	0.73	1.09	1.35	-0.44
<b>C. Emerging Markets</b>						
Argentina	-0.34	1.04	1.28	2.19	4.15	-4.49***
Brazil	-0.27	1.91	2.17	2.65	2.53	-2.80***
India	1.89	1.24	2.23	1.88	1.80	-0.09
Indonesia	1.51	2.55	2.18	3.10	3.76	-2.25***
Israel	0.32	0.97	1.72	2.10	2.46	2.14
Korea	-0.37	0.19	1.83	2.79	5.71	-6.08***
Malaysia	1.45	0.65	1.61	2.02	2.82	-1.37
Mexico	0.56	0.98	1.48	1.90	2.16	-1.50
Philippines	1.96	2.99	2.27	2.75	5.23	-3.27***
Poland	1.85	1.52	2.29	0.62	1.47	0.38
Russia	1.02	2.06	0.64	0.98	2.92	-1.88
South Africa	1.60	1.17	0.99	1.22	1.61	-0.01

(Continued)

**TABLE 5. (Continued)**

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Taiwan	0.92	0.48	0.96	1.76	2.17	-1.25
Thailand	0.61	1.00	0.51	1.30	1.65	-1.04
Turkey	1.78	1.94	1.88	2.197	2.42	-0.64

**Note:** Value-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the five-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column “Q1 – Q5” reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

TABLE 6. Countries Idiosyncratic Volatility in reference to the Four-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>A. G7 Countries</b>						
Canada	1.87	0.14	1.39	0.30	1.26	0.63
France	0.45	-0.07	0.56	0.16	-0.05	0.50
Germany	2.90	1.72	0.88	0.43	0.30	2.60***
Italia	1.44	0.13	1.04	0.71	1.38	0.06
Japan	1.53	0.65	0.60	0.66	1.32	0.21
United Kingdom	0.30	0.12	0.40	0.74	0.62	-0.32
United States	1.39	0.78	0.74	1.26	1.65	-0.16
<b>B. Developed Markets</b>						
Australia	0.03	3.44	-3.89	-0.88	0.87	-0.90
Austria	0.03	0.41	0.90	1.44	1.16	-1.19
Belgium	1.03	0.21	0.39	1.18	1.64	-0.61
Denmark	1.06	1.32	1.48	0.42	0.81	0.25
Finland	-0.24	2.23	1.94	0.93	1.28	-1.52
Greece	0.99	0.86	1.93	1.88	2.29	-1.30
Hong Kong	2.49	1.58	1.07	2.01	2.91	-0.52
Ireland	1.13	1.19	1.12	1.90	1.94	-0.81
Netherlands	1.72	0.47	0.78	1.47	1.51	0.21
New Zealand	1.28	0.65	0.11	-0.03	0.64	0.64
Norway	0.08	2.05	2.23	1.82	1.89	1.81
Portugal	-1.04	-0.02	1.35	0.50	1.51	-2.55

(Continued)

TABLE 6. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	2.73	1.16	1.07	1.05	1.74	0.99
Spain	-0.010	0.009	0.013	0.011	0.009	-0.019
Sweden	1.58	0.81	2.17	1.48	2.37	-0.79
Switzerland	0.94	0.90	0.82	0.99	1.34	-0.40
<b>C. Emerging Markets</b>						
Argentina	-0.26	1.23	1.82	2.27	3.97	-4.23***
Brazil	0.09	1.58	2.55	2.52	2.58	-2.49***
India	1.89	1.24	2.28	1.88	1.80	-0.09
Indonesia	1.36	2.72	2.52	3.20	4.20	-2.84***
Israel	0.46	0.83	2.19	2.26	2.35	-1.89
Korea	-0.29	0.05	1.87	2.89	5.76	-6.05***
Malaysia	0.71	1.14	1.82	2.32	2.60	-1.89
Mexico	0.81	1.03	1.45	2.76	2.04	-1.23
Philippines	1.73	3.61	2.59	3.26	4.94	-3.21***
Poland	1.46	1.04	2.99	1.14	1.37	0.09
Russia	1.02	1.72	0.97	0.87	2.21	-1.19
South Africa	1.86	0.92	1.08	0.96	1.85	0.01

(Continued)

TABLE 6. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Taiwan	1.11	0.44	1.00	1.77	2.07	-0.96
Thailand	0.88	0.74	0.65	1.54	1.75	-0.87
Turkey	1.85	2.08	1.56	1.64	2.61	-0.76

**Note:** Value-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the four-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column "Q1 – Q5" reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.



TABLE 7. Countries Idiosyncratic Volatility in reference to the Three-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>A. G7 Countries</b>						
Canada	2.93	1.33	1.18	1.39	0.46	2.47***
France	2.67	0.68	0.90	1.11	1.26	1.41***
Germany	1.97	0.81	0.99	0.957	1.12	0.85
Italia	2.27	0.07	0.79	0.58	0.89	1.38***
Japan	1.57	0.33	0.29	0.35	0.56	1.01
United Kingdom	1.22	1.04	0.86	0.97	1.03	0.19
United States	1.59	1.60	1.01	0.92	1.38	0.21
<b>B. Developed Markets</b>						
Australia	2.08	1.42	0.81	1.08	0.82	1.26
Austria	0.65	0.57	0.88	0.87	0.95	-0.30
Belgium	1.07	1.01	0.94	0.52	0.66	0.41
Denmark	0.95	1.09	0.98	1.34	1.77	-0.82
Finland	0.40	0.76	0.67	1.24	1.57	-1.17
Greece	0.72	2.49	1.17	1.04	1.70	-0.98
Hong Kong	2.37	2.21	1.64	1.53	2.45	-0.08
Ireland	1.63	1.21	0.40	1.438	1.28	0.35
Netherlands	1.20	0.67	0.73	0.69	0.16	1.04
New Zealand	1.28	0.77	0.74	0.65	0.71	0.57
Norway	1.16	2.35	2.12	1.55	1.05	0.11
Portugal	-1.32	-0.41	0.65	0.78	1.20	-2.52

(Continued)

TABLE 7. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	3.04	1.10	1.23	1.08	1.30	1.74
Spain	-0.01	0.004	-0.003	-0.003	0.025	-0.026
Sweden	2.06	1.10	1.14	1.26	1.60	0.46
Switzerland	1.23	0.80	0.78	0.91	1.12	0.11
<b>C. Emerging Markets</b>						
Argentina	0.10	0.08	0.39	1.39	5.11	-5.01***
Brazil	-0.07	1.57	2.15	2.37	2.55	-2.62***
India	2.00	2.21	2.22	2.59	2.87	-0.87
Indonesia	-0.58	0.32	0.51	2.22	5.26	-5.64***
Israel	0.24	1.11	1.50	1.67	2.35	2.11
Korea	0.38	1.48	2.00	1.96	3.43	-3.05***
Malaysia	1.39	0.66	1.00	1.34	1.78	-0.39
Mexico	1.10	0.86	1.53	2.76	3.06	-1.96
Philippines	1.15	3.37	1.45	1.84	4.34	-3.19***
Poland	1.65	1.78	1.31	1.46	1.51	0.38
Russia	1.20	2.24	1.94	2.17	2.52	0.14
South Africa	1.82	1.63	1.47	1.70	2.10	-0.18

(Continued)

**TABLE 7. (Continued)**

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Taiwan	0.55	0.54	0.96	1.30	1.89	-1.34
Thailand	1.38	0.36	1.21	2.06	2.46	-1.08
Turkey	1.93	2.23	1.84	2.10	1.40	0.53

**Note:** Equally-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the three-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column “Q1 – Q5” reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

TABLE 8. Countries Idiosyncratic Volatility in reference to the Three-Factor Model

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>A. G7 Countries</b>						
Canada	1.79	-0.29	1.98	0.05	-0.94	2.73***
France	0.45	-0.05	0.27	0.21	-0.10	0.55
Germany	2.48	2.06	0.91	-0.24	0.07	2.41***
Italia	1.48	0.09	0.64	0.77	1.43	0.05
Japan	1.46	0.63	0.76	0.61	0.27	1.19
United Kingdom	1.38	0.03	0.50	0.71	0.69	0.69
United States	1.52	1.29	1.18	1.26	1.42	0.10
<b>B. Developed Markets</b>						
Australia	1.17	5.46	0.86	-2.70	-1.64	2.74**
Austria	-0.22	0.34	0.76	1.33	1.49	-1.71
Belgium	1.06	0.08	0.18	0.93	1.82	-0.76
Denmark	1.06	1.01	1.11	1.00	0.77	0.29
Finland	-0.30	2.28	1.06	1.28	1.38	-1.52
Greece	0.09	1.15	0.91	1.15	1.76	-1.67
Hong Kong	-0.39	1.63	1.26	2.06	1.83	-2.22
Ireland	0.19	1.36	0.63	1.59	1.84	-1.65
Netherlands	0.81	0.49	1.03	1.21	1.80	-0.99
New Zealand	1.24	0.53	0.51	0.35	0.52	0.72
Norway	0.08	2.70	1.82	1.80	1.75	-0.67
Portugal	-1.16	-0.02	1.22	0.35	1.67	-2.73

( Continued )

TABLE 8. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
<b>B. Developed Markets</b>						
Singapore	2.55	1.14	1.08	1.10	1.70	0.85
Spain	-0.010	0.008	0.011	0.010	0.008	-0.018
Sweden	1.46	1.01	1.22	1.46	2.35	-0.89
Switzerland	0.76	0.91	0.79	1.01	1.34	-0.58
<b>C. Emerging Markets</b>						
Argentina	-0.58	1.11	1.15	2.40	4.27	-4.85***
Brazil	0.04	1.57	2.08	2.72	2.45	-2.41***
India	1.05	-0.20	1.55	1.383	1.80	-0.75
Indonesia	2.00	2.67	2.21	2.74	4.37	-2.37***
Israel	0.84	0.72	1.64	2.31	2.60	-1.76
Korea	-0.38	0.35	1.56	2.93	6.07	-6.45***
Malaysia	1.45	0.65	1.61	2.02	2.82	-1.37
Mexico	0.53	1.27	1.27	2.29	2.64	-2.11
Philippines	1.10	4.27	2.16	3.74	4.43	-3.33***
Poland	1.62	0.96	2.53	1.04	1.41	0.21
Russia	1.51	1.70	0.79	0.99	2.47	-0.96
South Africa	1.80	1.19	0.89	1.33	1.55	0.25
Taiwan	0.72	0.33	1.14	1.64	2.24	-1.52

(Continued)

TABLE 8. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
C. Emerging Markets						
Thailand	-0.16	1.11	0.18	1.56	2.04	-2.20
Turkey	1.80	2.16	2.04	1.82	2.58	-0.78

**Note:** Value-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the three-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column "Q1 – Q5" reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

TABLE 9. Countries Idiosyncratic Volatility in reference to the Four-Factor Model – Subsamples

Country	Q1	Q2	Q3	Q4	Q5	Q1 – Q5
1 <sup>st</sup> Subsample						
A. G7 Countries						
Canada (1980 – 1996)	2.08	1.42	1.09	1.19	2.89	-0.81
France (1980 – 1996)	0.80	0.93	0.51	0.80	1.13	-0.33
Germany (1980 – 1996)	1.18	0.85	0.80	0.91	0.47	0.72
Italy (1986 – 1999)	2.92	1.24	-0.23	1.35	1.40	1.52
Japan (1980 – 1996)	3.41	0.90	0.94	0.63	1.24	2.17***
United Kingdom (1980 – 1996)	1.60	-0.01	1.77	1.44	-0.11	1.72
United States (1980 – 1996)	1.27	1.68	1.24	2.05	2.91	-1.65
B. Developed Markets						
Australia (1984 – 1998)	2.92	1.24	-0.23	1.35	1.91	1.01
Belgium (1986 – 1999)	1.63	0.18	0.11	0.23	0.39	1.24
Hong Kong (1988 – 2000)	0.98	1.45	1.54	-0.19	1.88	-0.90
Netherlands (1980 – 1996)	0.83	1.12	1.14	1.15	0.44	0.39
Singapore (1989 – 2001)	2.89	0.17	-0.02	-0.20	0.19	2.70**
Switzerland (1980 – 1996)	0.76	0.68	0.60	0.54	0.29	0.46
C. Emerging Markets						
Korea (1987 – 1999)	0.57	0.33	-1.40	0.24	2.75	-2.18***
Malaysia (1986 – 1999)	0.09	0.22	0.40	0.11	1.35	-1.26

( Continued )

TABLE 9. (Continued)

Country	Q1	Q2	Q3	Q4	Q5	Q1 - Q5
2 <sup>nd</sup> Subsample						
A. G7 Countries						
Canada (1980 - 1996)	3.83	1.26	1.37	1.31	1.77	2.07
France (1980 - 1996)	4.56	0.36	1.20	1.10	1.05	3.51**
Germany (1980 - 1996)	2.85	0.79	1.27	0.93	1.49	1.36**
Italy (1986 - 1999)	1.52	-1.02	1.87	-0.59	-0.18	1.70
Japan (1980 - 1996)	-0.27	-0.23	-0.36	0.07	-0.11	-0.15
United Kingdom (1980 - 1996)	0.84	2.09	1.07	0.72	2.21	-1.38
United States (1980 - 1996)	1.97	1.22	1.26	0.38	0.45	1.53
B. Developed Markets						
Australia (1984 - 1998)	1.34	1.70	1.93	1.41	1.33	0.01
Belgium (1986 - 1999)	0.51	2.00	1.49	1.01	0.91	-0.40
Hong Kong (1988 - 2000)	3.54	3.05	1.46	3.85	2.46	1.08
Netherlands (1980 - 1996)	1.57	0.24	-0.03	0.59	0.10	1.47
Singapore (1989 - 2001)	3.57	1.93	2.54	2.48	2.49	1.08
Switzerland (1980 - 1996)	1.70	0.94	0.70	0.81	0.92	0.16
C. Emerging Markets						
Korea (2000 - 2012)	-0.27	2.61	4.47	3.06	1.67	-1.94
Malaysia (2000 - 2012)	1.13	1.58	1.46	3.43	2.75	-1.62

(Continued)



**TABLE 9. (Continued)**

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**Note:** Equal-weighted quintile portfolios are formed every month by sorting stocks based on idiosyncratic volatility relative to the four-factor model. Portfolios are formed every month, based on volatility computed using daily data over the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The column “Q1 – Q5” reports the difference in monthly returns between portfolio 1 and portfolio 5. \*\* denotes significance at 5% level. \*\*\* denotes significance at 1% level.

developed countries.

In panel C of tables 7 and 8, the results when idiosyncratic volatility is estimated in respect to the three-factor model remain again similar to the ones exhibited in tables 3 to 6: Most of the emerging markets provide evidence of a positive relationship (11 and 13 for equal- and value-weighted portfolios respectively) and 5 out of these 15 countries imply a statistically strong association.

In summary, the relation between idiosyncratic risk and expected returns when idiosyncratic volatility is estimated using the five and four-factor models is ambiguous. For equal-weighted portfolios, a strong and negative relationship is observed for 3 of the G7 countries: France, Germany and Japan, an idiosyncratic volatility trading strategy of going long on low idiosyncratic volatility stocks and short on high idiosyncratic stocks can generate economically and statistically significant trading profits. For value-weighted portfolios, this same trading strategy would be profitable for Canada and Germany only.

While developed markets present insignificant mixed results, some emerging markets (5 out of 16 countries) provide evidence of a strong positive relation between expected returns and past idiosyncratic volatility. For these countries, an investment strategy of buying high idiosyncratic volatility stocks and shorting low idiosyncratic volatility stocks could result in significant trading profits.

The majority of the countries analyzed in this paper (2, 3 or 4 of the G7 countries depending on the weighting, all developed countries and 11 of the 16 emerging markets) present no evidence of a relationship between diversifiable risk and expected returns. These findings are in contrast to the ones observed by Ang et al. (2009) in which all countries in their study show a negative correspondence between idiosyncratic volatility and expected returns.

## V. Conclusion

This study examines the role of idiosyncratic risk in an international context motivated by the study of Ang et al. (2006) that reveals the presence of an abnormal negative relationship between realized idiosyncratic volatility and subsequent 1-month stock returns. This negative relationship has been successively denoted to in the literature

as the ‘idiosyncratic volatility puzzle’ with the possibility that this anomaly might be international following evidence reported by Ang et al. (2009) in the US and 22 other developed markets. The Ang et al. (2006) framework is expanded to estimate the impact of idiosyncratic risk in international stock markets using two additional asset pricing models to estimate diversifiable risk i.e. the Carhart four-factor model as well as the five-factor model (four-factor model plus the Amihud liquidity factor).

The results obtained suggest that idiosyncratic risk does not play a role on stock returns for the 16 developed markets analyzed. While some evidence of a negative link between idiosyncratic risk is shown, the relation is statistically significant for only a few of the G-7 countries in the analysis. Indeed, only Germany shows a monotonic negative relationship between idiosyncratic volatility and stock market returns, consistent with Koch (2010). It may be the case that this is due to the fact that equity markets are still not well developed in Germany, which persists as one of the most bank-based financial systems relative to other countries in the G-7. The relatively “thinner” equity market of German firms may in part explain the idiosyncratic volatility puzzle for Germany. Providing a more thorough and rational explanation of this result remains a matter for future research. We do note, on the other hand, that idiosyncratic volatility is positively related to future expected returns for 5 out of 15 emerging market countries.

The findings related to emerging countries are consistent with investor under-diversification (e.g., Levy (1978); and Merton (1987)) wherein investors request a premium for taking idiosyncratic risk. This under-diversification may be due to informational efficiencies, although liquidity risk per se does not seem to be a driving factor in explaining the divergent results between developed and emerging markets.

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Appendix 1. Illustrative Stocks in various countries used in the analyses

Canada	G-7				Developed			Emerging		
	Germany	United States	Australia	Hong Kong	Sweden	Brazil	Mexico	Taiwan		
Astral Media	Adidas	Baxter Intl.	Adelaide Brighton	Aac Technologies	Aarhuskarlshamn	Aes Tiete Pn	Aeromex	Acer		
Bank of Montreal	Allianz	Boeing	Caltex Australia	Bank of East Asia	Atrium Ljungberg 'B'	Banco Brasil On	Bolsa 'A'	Compal Electronics		
Dollarama	Beiersdorf	First Amer.Finl.	Flexigroup	Cheung Kong Infr.Hdg	Elekta 'B'	Coelba On	Elektra	Far Eastern New Century		
Great West	Carl Zeiss	General Dynamics	Goodman Fielder	Foxconn Intl.Holdings	Hufvudstaden 'A'	Embraer On	Gfamsa 'A'	Farmosa Petrochemical		
Lifeco	Meditec	Humana	Invocare	Gcl-Poly Energy	Husqvarna 'B'	Localiza On	Gigante	Hon Hai Precn.Ind.		
Manulife Financial	Deutsche Bank	Johnson & Johnson	Linc Energy	Haier Electronics Gp.	Lundin Petroleum	Petrobras On	Gruma 'B'	Hua Nan Financial Hdg.		
Metro	Deutsche Telekom	Lennox Intl.	Nufarm	Hongkong & Shai Htlls.	Melker Schorling	Santander Br Pn	Invex 'A'	Novatek Microels.		
Nat.Bk.of Canada	Diskus Werke	Morgan Stanley	Qantas Airways	Lenovo Group	Skanska 'B'	Santos Brp Unit	Lamosa	Quanta Computer		

( Continued )

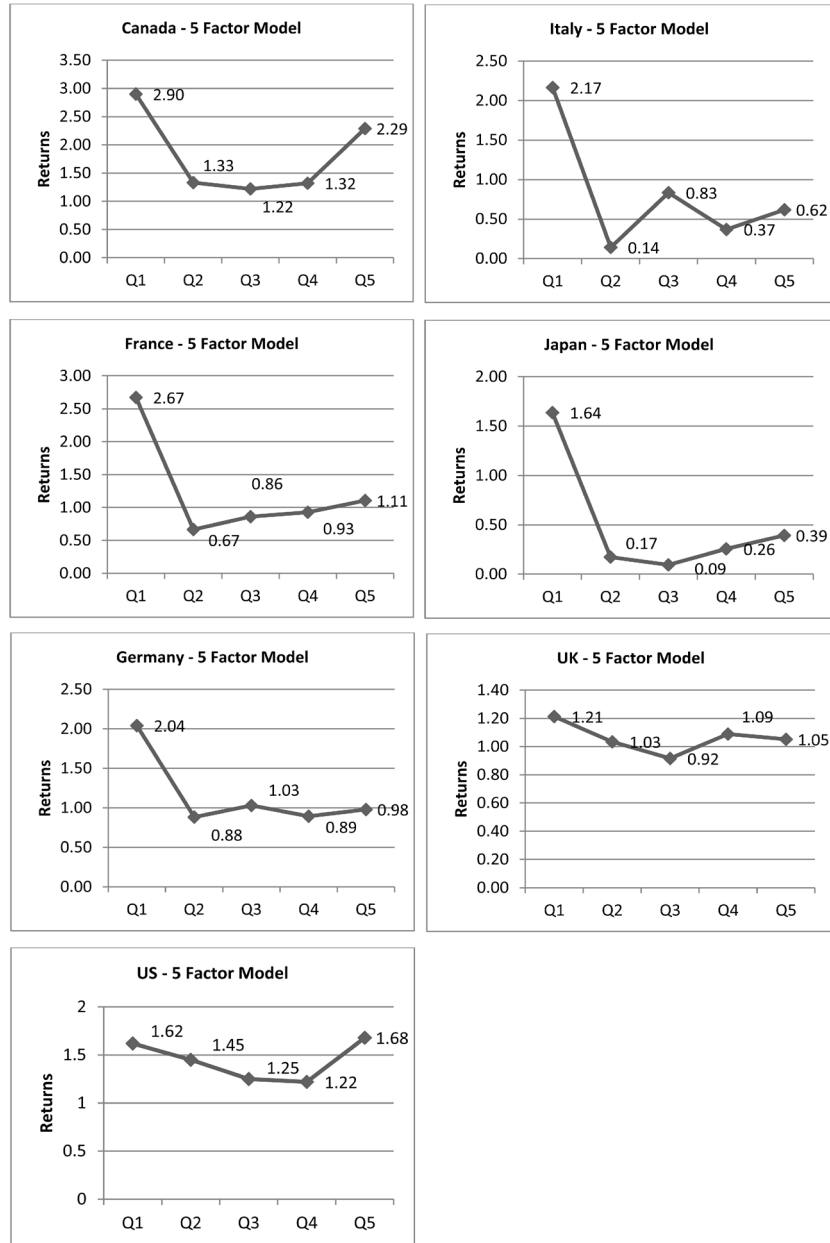
**Appendix 1. (Continued)**

	G-7						
	Germany	United States	Australia	Hong Kong	Sweden	Brazil	Mexico
Canada							
Paladin Labs	Infineon Technologies	Public Storage	Southern Cross Media Gp.	Nws Holdings	Svenska Handbkn. 'A'	Telef Brasil On	Sanmex 'B'
Rogers Comms. 'B'	Koenig & Bauer	Sysco	Telstra	Sino Biophm.	Teliasonera	Usiminas On	Soriana 'B'
Royal Bank of Canada	Salzgitter	Tyco International Group	Transurban Group	Tsim Sha Tsui Proprs.	Volvo 'B'	Vale Pna	Tlevisa 'Cpo'
Weston George	Thyssenkrupp	Xerox	Westpac Banking	Xinyi Class Holdings	Withborgs Fastigheter	Via Varejo On	Walmex 'V'
							Taiwan Mobile
							Skin Kong Finl.Hldg.
							Synnex Tech.Intl
							Taishin Financial Hldg.

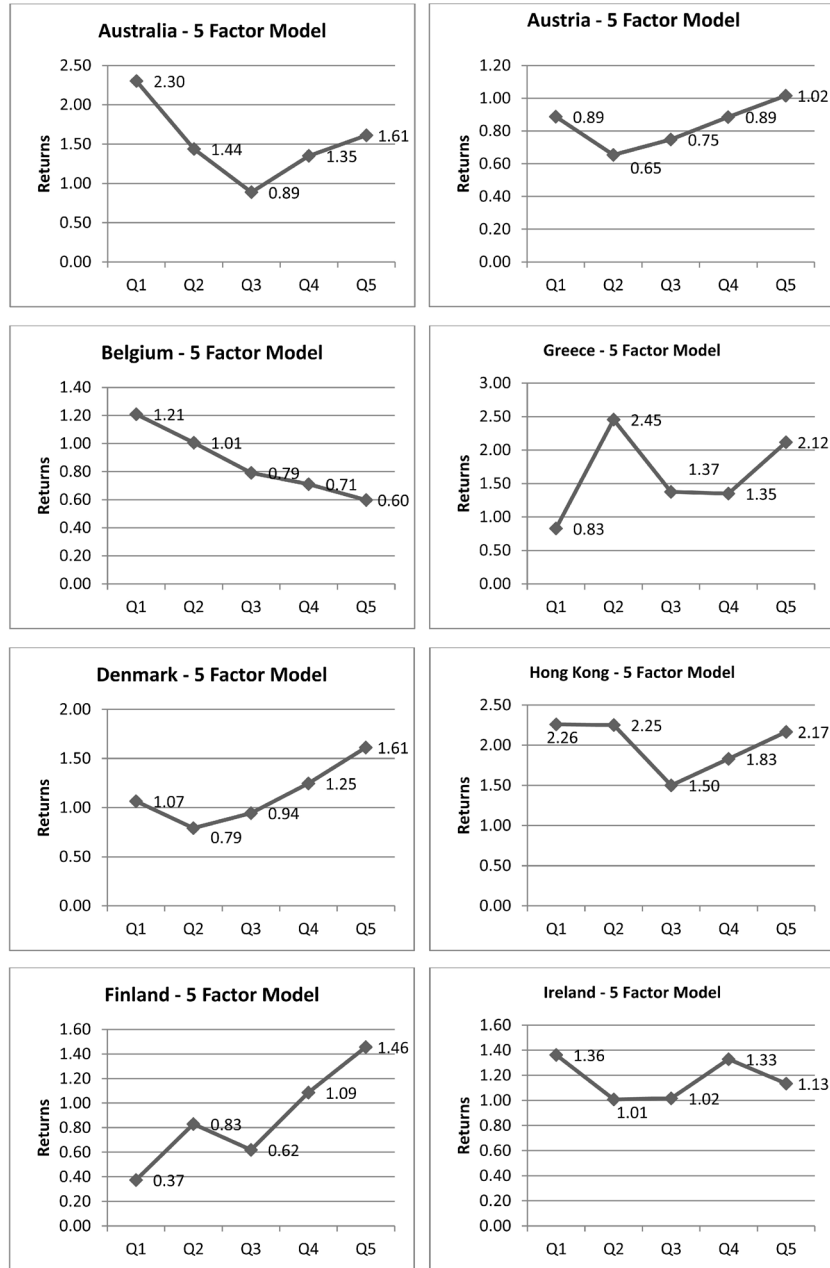
**Note:** The list of all countries in each group (G7 vs. Developed vs. Emerging) from which these companies were obtained is provided in table 1.

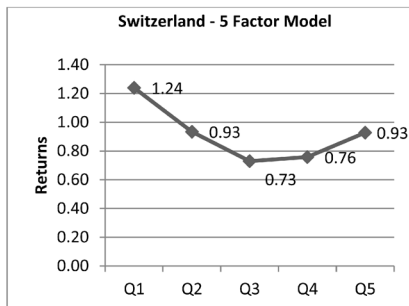
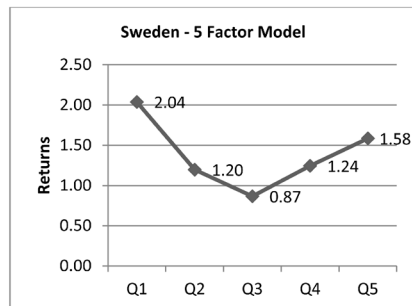
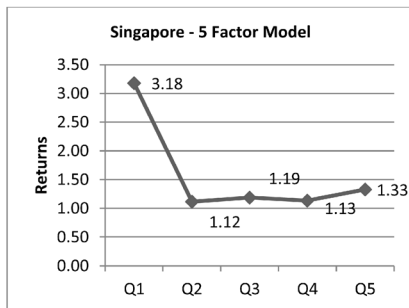
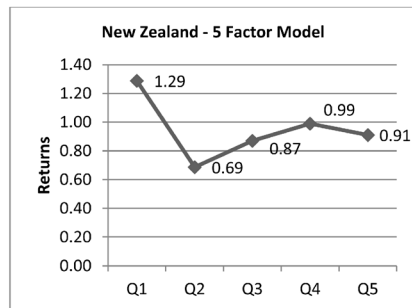
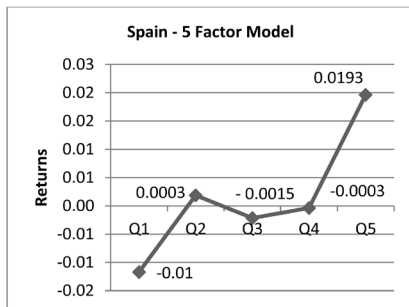
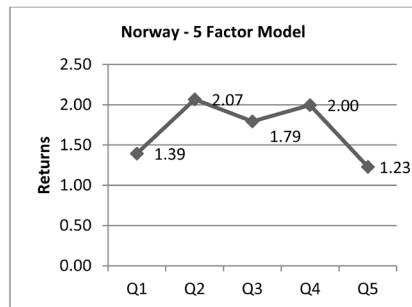
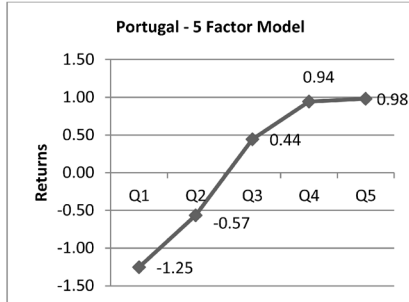
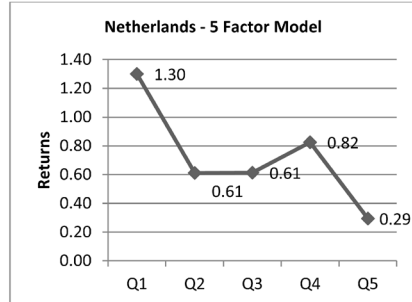
**Appendix 2: Equal-Weighted Portfolio Returns Sorted According to Idiosyncratic Volatilities**

**A. G7 Countries**



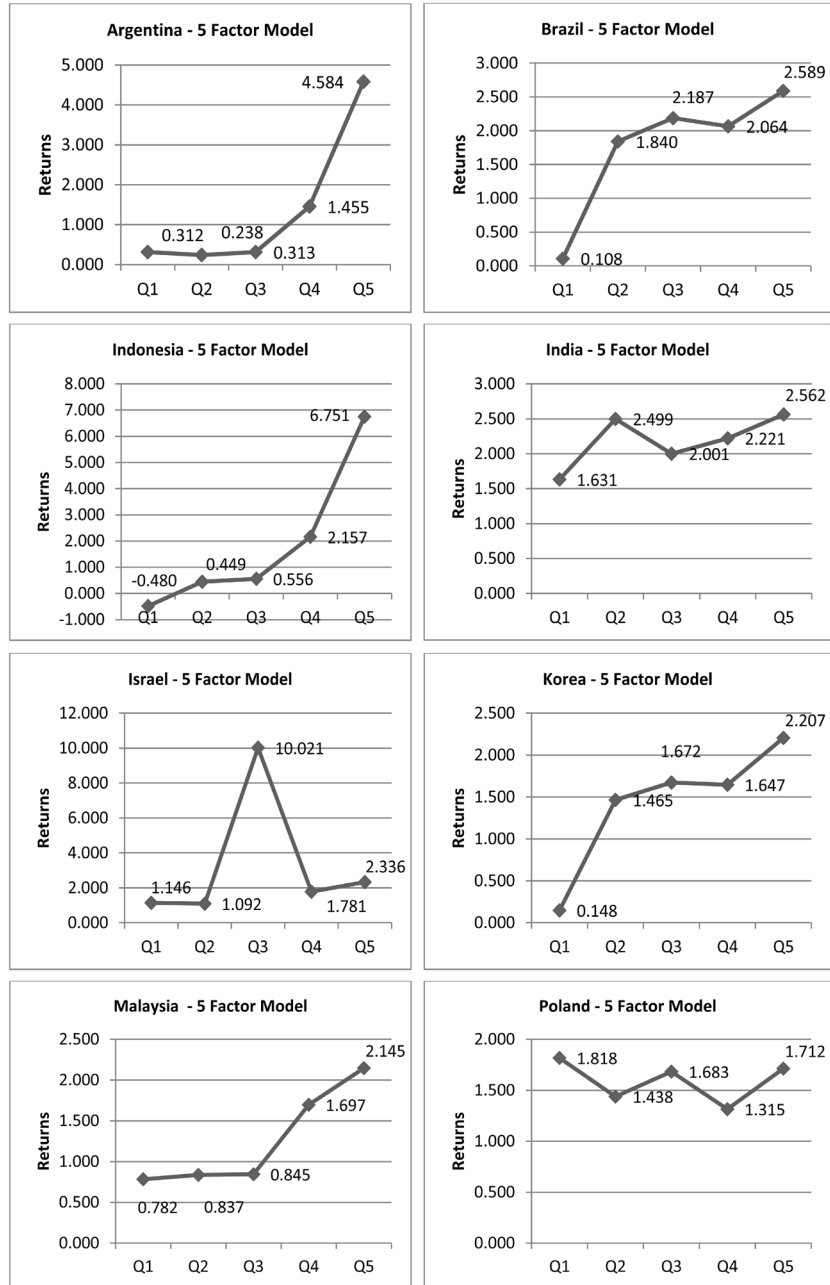
**B. Other Developed Countries**

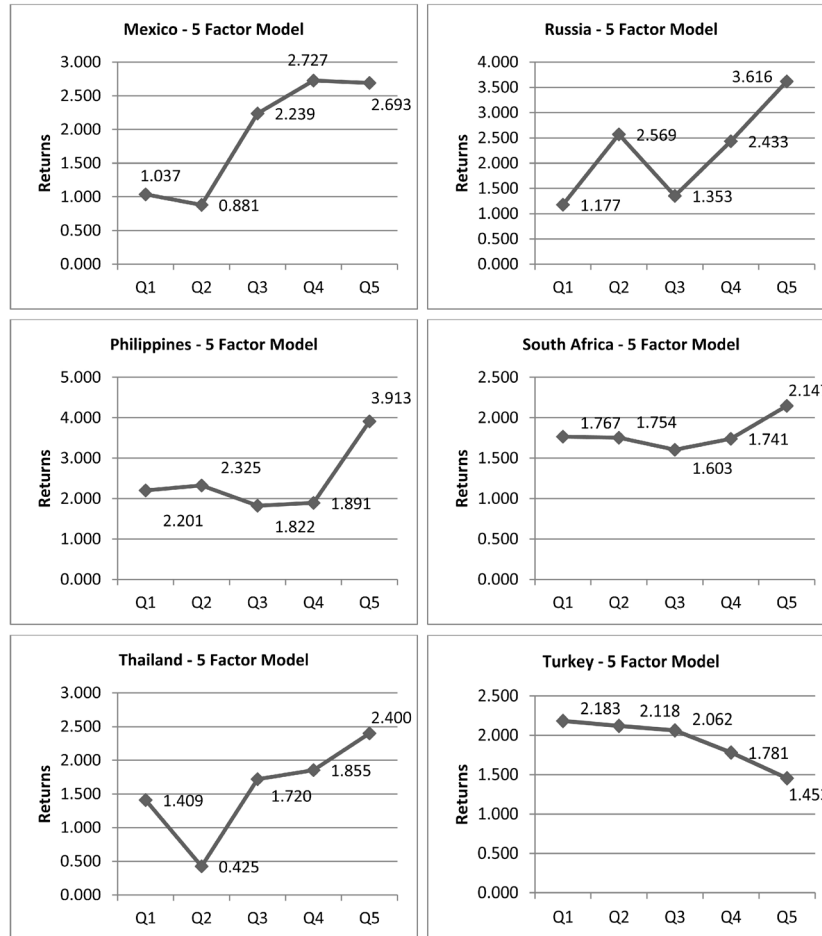






C. Emerging Countries





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